Ve401 Probabilistic Methods in Engineering

Summer 2017 Term Project 2

Date Due: 12:00 PM, Friday, the 4th of August 2017

General Information

The goal of this term project is to help you apply your new-found knowledge of probability theory and statistics in extended tasks that are beyond the scope of ordinary assignments. Although the project is published early, you will find that the tasks require techniques that are treated as the term progresses, so that you will be able to complete the project gradually. It is strongly recommended that you do not leave the entire project to the last minute but rather commence work on individual parts as soon as you are able to do so.

Group Work

You will be divided into groups of 4-5 students each.

Each group member must be familar with and have contributed to each part of the project report. You may not divide up the work in such a way that only certain members are invovled with certain parts. In the event of an Honor Code violation (plagiarism or other), all members of the group will be held equally responsible for the violation. Exceptions may only be made, at my discretion, only in extreme circumstances.

It is therefore all group members' duty to ensure that all collaborators' contributions are plausibly their own and to check on all collaborators' work progress and verify their contributions within reason.

Project Report

The term project will be submitted as a typed report both electronically and as a hard copy printout. Handwritten submission will not be accepted! It is recommended that you use a professional type-setting program (such as LATEX) for your report. Unless you are able to ensure a unified font size and style for formulas and text in Microsoft Word, use of Word is not recommended.

Grading Policy

This term project accounts for 25% of the course grade; it will be scored based on

- Form: Does the report contain essential elements, such as a cover page (with title, date, list of authors), a synopsis (abstract giving the main conclusions of the project), table of contents, introduction, clear division into sections and appendices with informative titles and bibliography (if applicable)? Are the printout pages professionally bound or just a collection loose or stapled sheets? Are the pages numbered? Are the text and formulas composed in a unified font? Are all figures (graphs and images) clearly labeled with identifiable source?
- Language: Is the style of english appropriate for a technical report? Do not treat the project as an assignment and simply number your results like part-exercises. Your text should be a single, coherent whole.

Errors in grammar and orthography (use a spell-checker!) will be penalized. Make sure that the report is interesting to read. Avoid simply repeating sentences by cut-and-paste. If in doubt about a formulation, contact me well before the submission date and I will help you with the language.

• Content: Are the mathematical and statistical methods employed clearly identifiable? Have they been justified (e.g., model assumptions)? Are the conclusions well-supported by the mathematical analysis? Is the methodology careful, appropriate and well-documented?

All group members will receive the same grade for the term project. (Exceptions are possible in special circumstances.)



On Plagiarism

Study JI's Honor Code carefully. **Any** information from third parties (books, web sites, even conversations) that you use in your project must be accounted for in the bibliography, with a reference in the text. Follow the rules regarding the correct attribution of sources that you have learned in your English course (e.g., Vy100, Vy200). All members of a group are jointly responsible for the correct attribution of all sources in all parts of the project essay, i.e., any plagiarism will be considered a violation of the Honor Code by all group members. Every group member has a duty to confirm the origin of any part of the text.

The following list includes some specific examples of plagiarism:

- Use of any passage of three words or longer from another source without proper attribution. Use of any phrase of three words or more must be enclosed in quotation marks ("example, example, example"). This excludes set phrases (e.g., "and so on", "it follows that") and very precise technical terminology (e.g., "without loss of generality", "reject the null hypothesis") that cannot be paraphrased,
- Use of material from an uncredited source, making very minor changes (like word order or verb tense) to avoid the three-word rule.
- Inclusion of facts, data, ideas or theories originally thought of by someone else, without giving that person (organization, etc.) credit.
- Paraphrasing of ideas or theories without crediting the original thinker.
- Use of images, computer code and other tools and media without appropriate credit to their creator and in accordance with relevant copyright laws.

Police Shootings in the United States

This part of the project is based on the article *London murders: a predictable pattern?* by David Spiegelhalter and Arthur Barnett [4]. The article is available for download from the *Resources* section of the SAKAI site. It analyzes the pattern of murders in London between April 2004 and September 2007 based on data of the London Metropolitan Police, obtained from the British Home Office.

Using data obtained from the *Database of Fatal Police Shootings* of the Washington Post [3] the occurrence of fatal police shootings in the US can be analyzed in manner analogous to that of Spiegelhalter and Barnett.

- i) Summarize the source of the data and characterize how the term "fatal police shooting" is used here.
- Use Mathematica to re-create a version of Figure 1 in [4] from the Police Shooting data between January 1st, 2015 and December 31st, 2016 available from https://github.com/washingtonpost/data-police-shootings. Note that one of the years covered by the data is a leap year decide how to treat February 29th.
- iii) From their data, Spiegelhalter and Barnett estimated that the London homicides follow a Poisson distribution with parameter k = 0.44. Using the police shooting data, test the hypothesis that the occurrence of police shootings in the US has followed a Poisson distribution in the years 2015 to 2016.
- iv) Recreate tables analogous to Table 1 (on page 3) and Figure 2 in [4] using your data.
- v) Create a table analogous to Figure 3 in [4] using Mathematica. Is there evidence that the average number of police shootings depends on the weekday?
- vi) Spiegelhalter and Barnett discuss the distribution of the "number of days without any homicides in London". Unfortunately, there are far too many police shootings for this to be practical here. Instead, find the predicted and actual number of days with n shootings, n = 0, 1, 2, 3, ... and create graphs analogous to Figures 4 a) and b) in [4], the absicssa giving n and the ordinate giving the (expected and observed, respectively) number of days with n shootings.
- vii) Confidence intervals for the parameer k of a Poisson distribution have been studied extensively; the survey [2] gives 19 different expressions! However, in our case we have a very large sample size and it is safe to assume that \overline{X} (the estimator for k) follows a normal distribution. In the spirit of the discussion of confidence intervals for proportions, show that a $(1 \alpha)100\%$ confidence interval for k is given by

$$\hat{k} \pm z_{\alpha/2} \sqrt{\hat{k}/n}$$

and calculate such an interval using the data of the years 2015 and 2016.

- viii) Using the data of 2017 to today, check whether it follows a Poisson distribution and calculate k_{2017} . Does this estimate fall into the confidence interval calculated above?
- ix) Prediction intervals for the number of observations are also well-studied (see [1] for example). Derive Nelson's formula [1, (18)], which is also valid under the assumption of large sample sizes and an approximate normal distribution of the estimator for k. Using this formula, obtain 95% prediction intervals for the number of police shootings based on the data for 2015 and 2016. Plot the data for both years in a single graph (using two different colors for the two years) along with the prediction intervals, mirroring Figure 5 in [4].
- x) Does the data for 2017 lie within the prediction intervals? Plot the cumulative number of police shootings together with the intervals obtained from the 2015 and 2016 data.

References

- K. Krishnamoorthy and Jie Peng. Improved closed-form prediction intervals for binomial and poisson distributions. Journal of Statistical Planning and Inference, 141(5):1709 – 1718, 2011.
- [2] VV Patil and HV Kulkarni. Comparison of confidence intervals for the poisson mean: some new aspects. REVSTAT-Statistical Journal, 10(2):211–227, 2012.
- [3] The Washington Post. Fatal force. https://www.washingtonpost.com/graphics/national/ police-shootings-2016/. Web. Accessed February 16th, 2017.
- [4] D. Spiegelhalter and A. Barnett. London murders: a predictable pattern? Significance, 6(1):5-8, 2009. http://onlinelibrary.wiley.com/doi/10.1111/j.1740-9713.2009.00334.x/abstract [Online; accessed 5-July-2015].